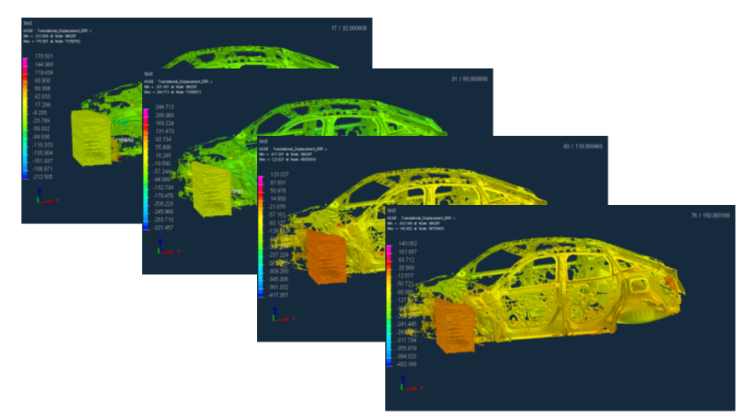


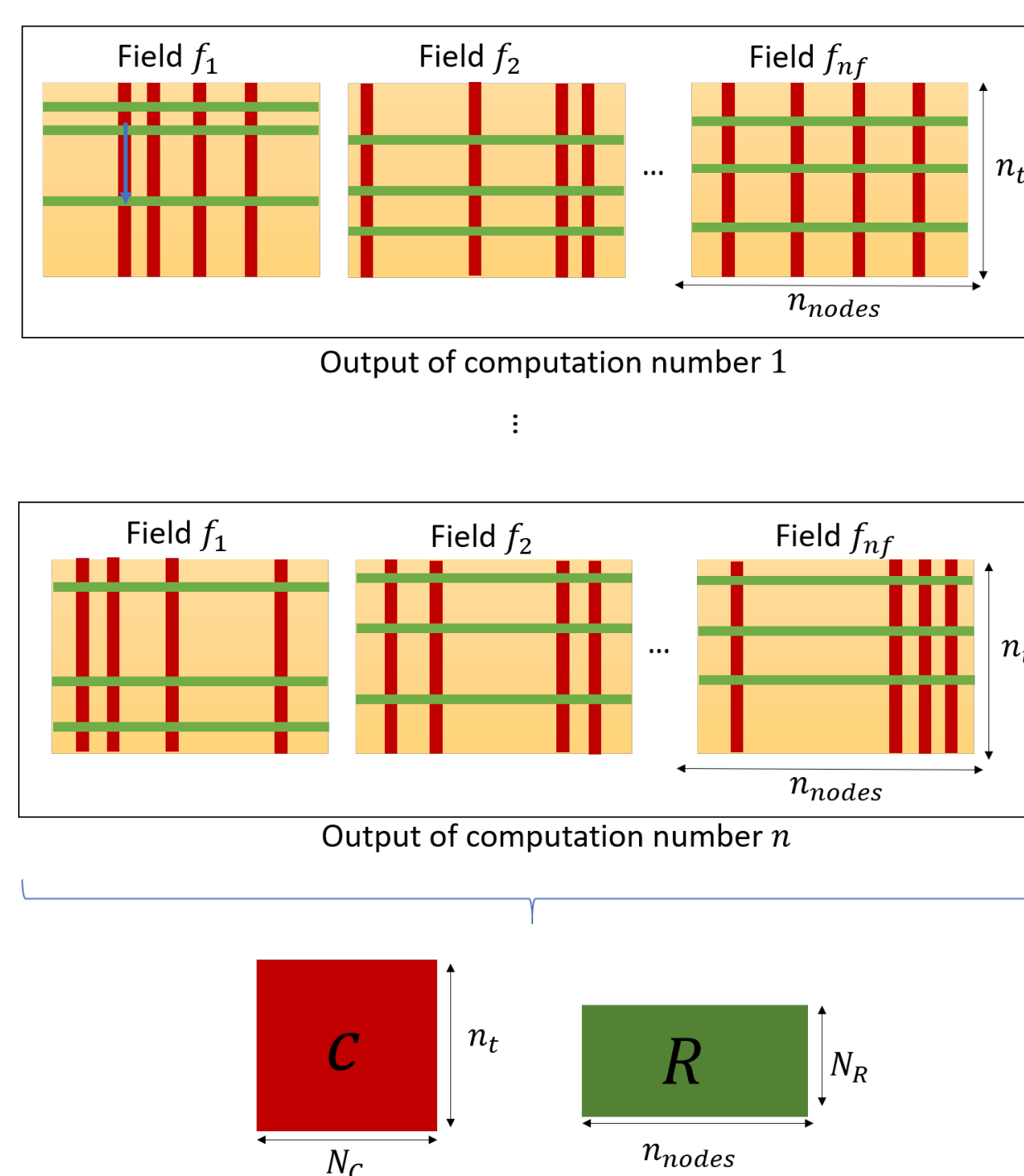
Classic optimization studies in vehicle projects are time and CPU consuming requiring hundreds of simulations. The aim of this project is to provide a new way to carry out optimization studies reducing dramatically the number of numerical simulations. [1]

A new method : Regression - CUR

1 Snapshots extraction from numerical simulations



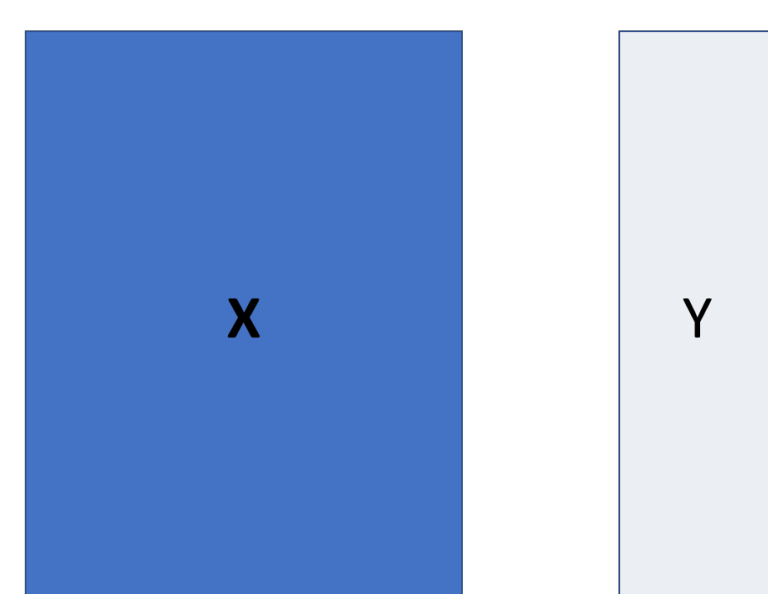
2 Data processing: « modes » extraction



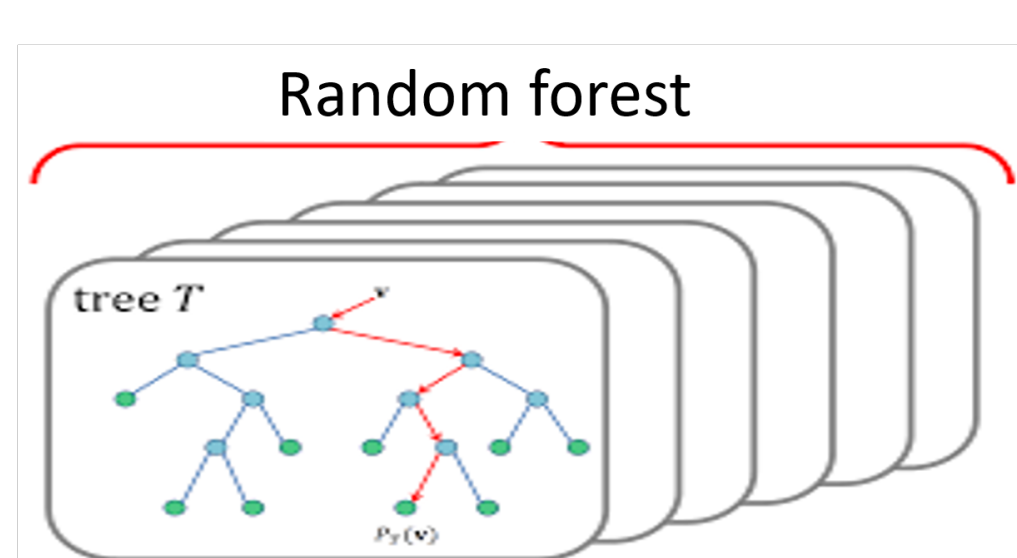
Modes selection methods

- kMeans clustering
- Empirical Interpolation Method [2]

3 Features and target building One sample = one node at one timestep of one field from one numerical simulation



4 Machine Learning model



Models that can be used

- Linear Regression
- Random Forest [1]
- Neural networks (future work)

Details of features construction in ReCUR

- A features matrix X_0 in which each line describes one node at a timestep is built.
- X_0 matrix is the basis containing all the extracted modes from the processed simulations.

$$\begin{bmatrix} C \\ \vdots \\ C \end{bmatrix} \begin{bmatrix} [R^T]_{1,n_r} \\ [R^T]_{2,n_r} \\ \vdots \\ [R^T]_{n_t,n_r} \end{bmatrix} = X_0$$

$n_t * n_{nodes}$

- To obtain the training set that will enable to learn structure behavior according to the design parameters, X_{C_k} matrices corresponding to each C_k simulation are built.

$$X_0 \xrightarrow{\text{Element-wise operator op}} \mu_{C_k}^v$$

$$(X_{C_k})_{ij} = (X_0)_{ij} \text{op} (\mu_{C_k}^v)_{lm}$$

$n_t * n_{nodes}$

$N_c + N_R$

\mathcal{V} = design parameter
 C_k = computation number k

Element-wise operator op = multiplication, inverse,...

$$X_{model} = \begin{bmatrix} X_{C_1} \\ \vdots \\ X_{C_k} \end{bmatrix}$$

$N_{features} = N_c + N_R$

$$\begin{bmatrix} Y_{C_1}^{f_1} & Y_{C_1}^{f_2} & \dots & Y_{C_1}^{f_{nf}} \\ \vdots & \vdots & \ddots & \vdots \\ Y_{C_k}^{f_1} & Y_{C_k}^{f_2} & \dots & Y_{C_k}^{f_{nf}} \end{bmatrix}$$

$n_t * n_{nodes} * n_f$

Possible n_f targets to be predicted independently or not

- Once the model is built, the future simulations will be predicted using the initial values of the design parameters.
- The prediction base $X_{prediction}$ is then built thanks to these values and the X_0 basis previously set, just as X_{model} .

Advantages of Random Forest

- Fast and cheap to implement (only few CPUs needed)
- Non linear model
- Highly scalable

Classic DOE versus Reduced Order Model Example in frontal crash with 20 parameters

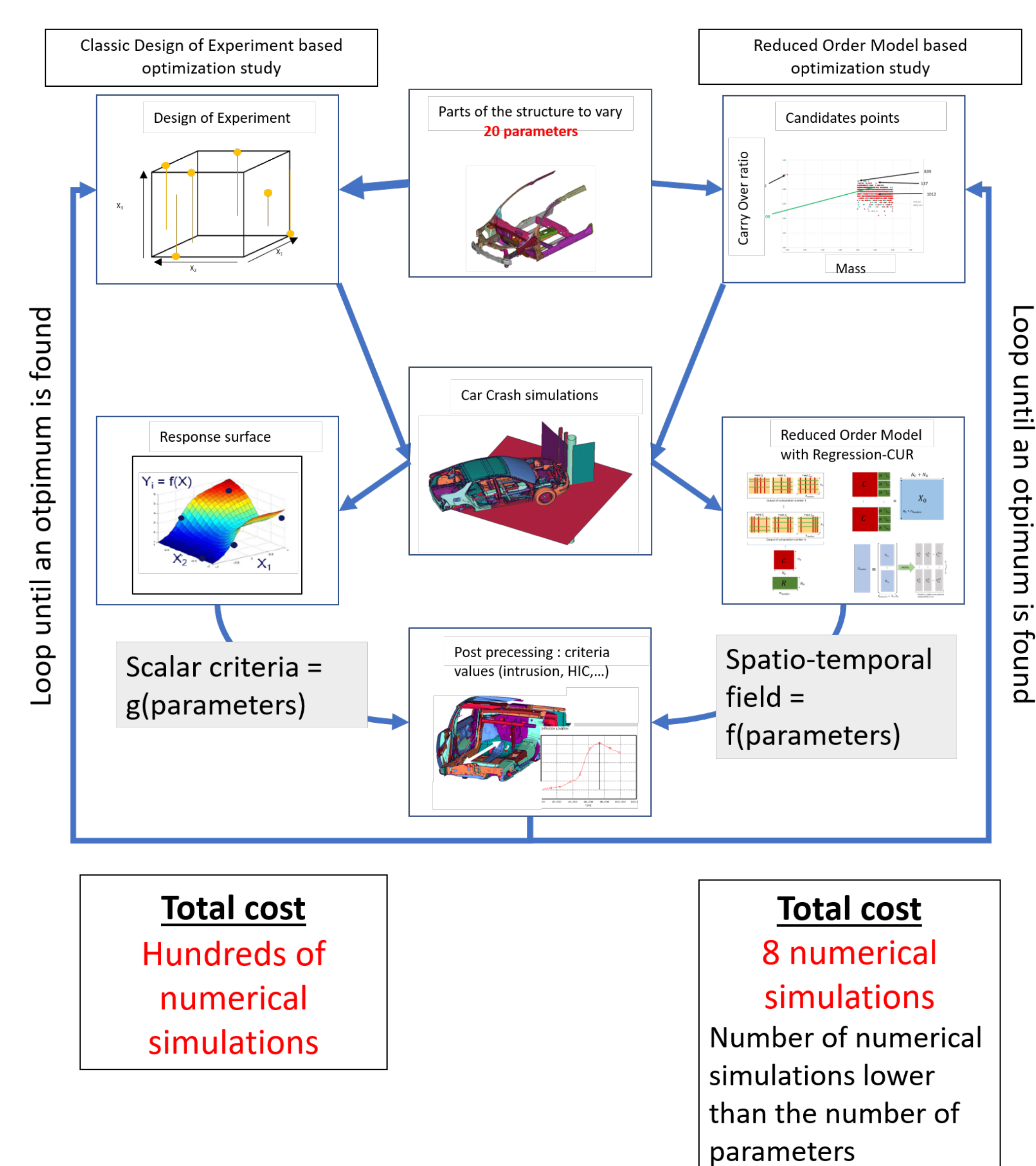
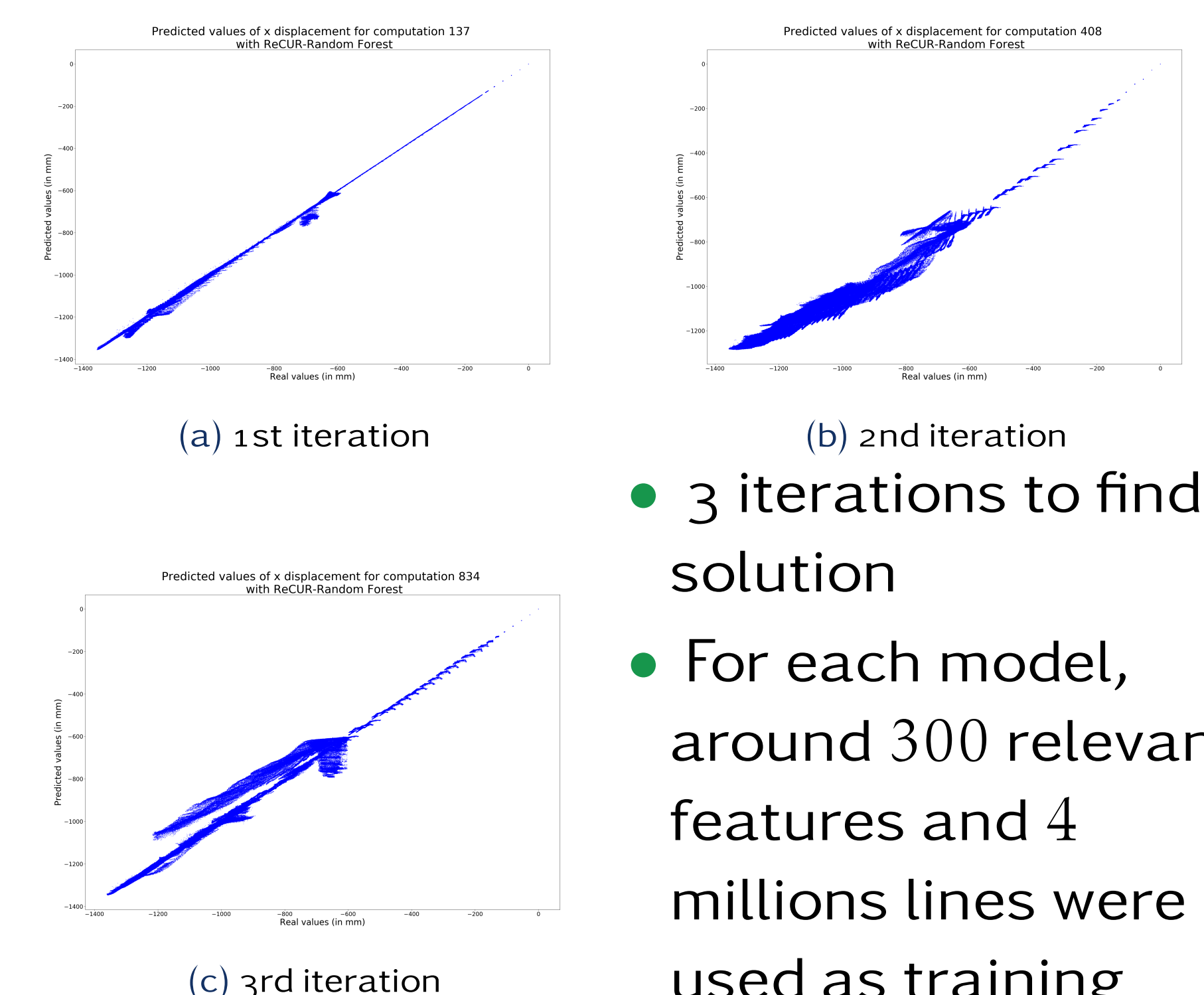


FIGURE – Quality of the three models when applied on a new configuration to predict. They are accurate enough to predict the specifications values and guide the optimization study.



- 3 iterations to find a solution
- For each model, around 300 relevant features and 4 millions lines were used as training data.

Conclusion

- An optimization study carried out with a number of simulations less than the number of parameters
- Non intrusive reduced order method that can be used in other physics context (combustion, NVH)

- [1] Sonia et al. A reduced model using random forest : Application on car crash optimization. *SeMA Journal*, 2019.
- [2] Gstalter et al. Towards disruptive methods for optimization study in automotive industry. *NaFEMS world*, 2019.